



Regulation R20

Subject code: 3B3AA

TKR COLLEGE OF ENGINEERING AND TECHNOLOGY

(Autonomous, Accredited by NAAC with 'A' Grade)

B.Tech III Semester Supplementary Examinations, July 2022 NUMERICAL METHODS

(Civil Engineering)

Maximum Marks: 70

Date:19.07.2022 Duration: 3 hours

- Note:
1. This question paper contains two parts A and B.
 2. Part A is compulsory which carries 20 marks. Answer all questions in Part A.
 3. Part B consists of 5 Units. Answer any one full question from each unit.
 4. Each question carries 10 marks and may have a, b, c, d as sub questions.

Part-A

All the following questions carry equal marks

(10x2M=20 Marks)

- 1 Find the reciprocal of 18 by using Newton-Raphson method. 2
- 2 Write a short notes on REGula- falsi method. 2
- 3 Find the relation between the operators E and D 2
- 4 Find the Lagrange's Interpolating polynomial fits the data 2

| | | | |
|------|---|---|----|
| x | 0 | 1 | 2 |
| f(x) | 2 | 1 | 12 |

- 5 Find dy/dx at x=1 from the table 2

| | | | | |
|---|---|---|----|----|
| x | 1 | 2 | 3 | 4 |
| y | 1 | 8 | 27 | 64 |

- 6 Evaluate $\int_0^1 x^3 dx$ by using Simpson's 3/8 rule, with n = 5. 2
- 7 Define initial and boundary value problems. 2
- 8 Compute y(0.1) for $dy/dx = xy + 1$ and $y(0) = 1$ using Taylor series method. 2
- 9 State Standard Five point formul and Diagonal Five point formula to solve a Poisson equation of second order. 2
- 10 Classify the equation 2

$$u_{xx} + 4u_{xy} + (4y^2 + x^2)u_{yy} = \sin(x+y)$$

Part-B

Answer All the following questions.

(5X10M=50Marks)

- 11 Derive a recurrence relation to find 5th root of a number. Hence find 5th root of 80 using Newton Raphson method. 10

OR

- 12 Find a +Ve real root of the equation $x \tan x + 1 = 0$ upto 2 decimals by Regula falsi method. 10

- 13 Use Newton forward interpolation formula to compute the pressure of the steam at temperature 142°C from the following steam table 10

| | | | | | |
|----------|-------|-------|-------|-------|--------|
| temp | 140 | 150 | 160 | 170 | 180 |
| Pressure | 3.685 | 4.854 | 6.302 | 8.076 | 10.225 |

OR

- 14 A curve passes through the points (0,18), (1,10), (3, -18), (6,90). Find the slope of the curve at $x = 2$. 10

- 15 Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ at $x = 1.5$ and $x = 4$

| | | | | |
|---|---|---|---|---|
| x | 1 | 2 | 3 | 4 |
| y | 3 | 5 | 6 | 7 |

OR

- 16 Evaluate $\int_0^{\pi} \frac{\sin x}{x} dx$ using $n = 6$, by a) Trapezoidal rule b) Simpson's 1/3 rule 10

- 17 Given $\frac{dy}{dx} = y^2 + 3x, y(0) = 1$ Find $y(0.1)$ taking $h = 0.1$ by using Taylor's series method. 10

OR

- 18 Apply 4th order Runge-Kutta method to find $y(0.1)$ given $y' = xy, y(0)=1$. 10

- 19 Find the numerical solution of the heat conduction equation $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} \quad 0 \leq x \leq 5, t > 0$ 10
with boundary conditions and initial conditions $u(0,t) = u(4,t) = 0$
 $u(x, 0) = x(5 - x)$.

OR

- 20 Applying Leibmann's iterative method, approximate the solution of Laplace equation $\nabla^2 u = 0$ with $h=1/3$ in a square mesh with vertices A(0,0), B(0,1), C(1,1) and D(1,0) 10
given that unknown function on the boundary is $u(x, y) = 9x^2y^2$